

# GROUPS OF ORDERS 97-100

## SUMMARY

order	<b>97</b>	<b>98</b>	<b>99</b>	<b>100</b>
# abelian	1	2	2	4
# other decomposable	0	1	0	6
# other indecomposable	0	2	0	6
<b>TOTAL</b>	<b>4</b>	<b>6</b>	<b>6</b>	<b>16</b>

$$97 = \langle A^{97} \rangle$$

$$98 = \langle A^{98} \rangle = 49 \times 2$$

$$98.2 = 14 \times 7 = \langle A^{14}, B^7 \rangle$$

$$98.3 = D_{14} \times 7 = \langle A^7, B^2, C^7, BA = A^{-1}B \rangle$$

$$98.4 = \langle A^7, B^7, C^2, CA = A^{-1}C, CB = B^{-1}C \rangle$$

CLASS EQUATION:  $98 = 1 + 2 \cdot 24 + 49$  #CC = 26

ORDER EQUATION:  $217 \cdot 2 = 2 \cdot 49 + 7 \cdot 48$

NORMAL SUBGROUPS:

H	<b>1</b>	<b>7</b>	<b>7<sup>2</sup></b>	<b>G</b>
G/H	<b>G</b>	<b>D<sub>14</sub></b>	<b>2</b>	<b>1</b>

$Z = \mathcal{N} = \Phi \times 7 \quad G' = 1$

Sylow subgroups:  $[2] \times 49$ ,  $[7^2]$  Maximal subgroups:  $[7^2]$ ,  $[D_{14}] \times 56$

$$98.5 = D_{98} = \langle A^{49}, B^2, BA = A^{-1}B \rangle$$

CLASS EQUATION:  $98 = 1 + 2 \cdot 24 + 49$  #CC = 26

ORDER EQUATION:  $1099 \cdot 2 = 2 \cdot 49 + 7 \cdot 6 + 49 \cdot 42$

NORMAL SUBGROUPS:

H	<b>1</b>	<b>7</b>	<b>49</b>
G/H	<b>G</b>	<b>D<sub>14</sub></b>	<b>2</b>

$Z = \mathcal{N} = \Phi \quad G'$

Maximal and Sylow subgroups:  $[2] \times 49$ ,  $[49]$

$$99 = \langle A^{99} \rangle = 11 \times 9$$

$$99.2 = 33 \times 3 = \langle A^{33}, B^3 \rangle$$

$$100 = \langle A^{100} \rangle = 25 \times 4$$

$$100.02 = 50 \times 2 = \langle A^{50}, B^2 \rangle$$

$$100.03 = 20 \times 5 = \langle A^{20}, B^5 \rangle$$

$$100.04 = 10^2 = \langle A^{10}, B^{10} \rangle$$

$$100.05 = D_{10} \times 10 = \langle A^5, B^2, C^{10}, BA = A^{-1}B \rangle$$

$$100.06 = 20.4 \times 5$$

$$100.07 = 20.5 \times 5$$

$$100.08 = 50.4 \times 2$$

$$100.09 = \langle A^2, B^5, C^5, D^2 = A, [B,D] = B^3, [C,D] = C^3 \rangle$$

CLASS EQUATION:  $100 = 1*2 + 2*24 + 25*2 \quad \#CC = 28$

ORDER EQUATION:  $281*2 = 2 + 4*50 + 5*24 + 10*24$

NORMAL SUBGROUPS:

H	1	2	5	10	5 <sup>2</sup>	10 × 5	G
G/H	G	50.4	D <sub>5,4</sub>	D <sub>10</sub>	4	2	1

$$Z = \mathcal{Z} = \Phi \quad \times 6 \quad \times 6 \quad G'$$

Sylow subgroups:  $[4] \times 25, [5^2]$

Maximal subgroups:  $[10 \times 5], [D_{5,4}] \times 30$

$$100.10 = D_{50} \times 2 = \langle A^{25}, B^2, C^2, BA = A^{-1}B \rangle$$

$$100.11 = \langle A^2, B^5, C^5 = B, D^2 = A, [B,D] = B^3, [C,D] = C^3B^4 \rangle$$

CLASS EQUATION:  $100 = 1*2 + 2*24 + 25*2 \quad \#CC = 28$

ORDER EQUATION:  $881*2 = 2 + 4*50 + 5*4 + 10*4 + 25*20 + 50*20$

NORMAL SUBGROUPS:

H	1	2	5	10	25	50	G
G/H	G	D <sub>50</sub>	D <sub>5,4</sub>	D <sub>10</sub>	4	2	1

$$Z = \mathcal{Z} \quad \Phi \quad G'$$

Sylow subgroups:  $[4] \times 25, [25]$

Maximal subgroups:  $[50], [D_{5,4}] \times 5$

$$100.12 = D_{10} \times D_{10} = \langle A^5, B^2, C^5, D^2, BA = A^{-1}B, DC = C^{-1}D \rangle$$

$$100.13 = \langle A^5, B^5, C^2, D^2 = C, [A,C] = A^3, [A,D] = A, [B,C] = B^3, [B,D] = B \rangle$$

**CLASS EQUATION:**  $100 = 1*2 + 2*4 + 4 + 12 + 25*3 \quad \#CC = 10$

**ORDER EQUATION:**  $185*2 = 2*25 + 4*50 + 5*24$

**NORMAL SUBGROUPS:**

H	1	5	5 <sup>2</sup>	50.4	G
G/H	G	M <sub>5,4</sub> <sup>(2)</sup>	4	2	1

$$Z = \mathcal{Z} = \Phi \quad \times 6 \quad G'$$

**Sylow subgroups:**  $[4] \times 25, [5^2]$

**Maximal subgroups:**  $[50.4], [M_{5,4}^{(2)}] \times 30$

$$100.14 = \langle A^5, B^5, C^2, D^2 = C, [A,C] = A^3, [A,D] = A, [B,C] = B^3, [B,D] = B^2 \rangle$$

**CLASS EQUATION:**  $100 = 1 + 4*6 + 25*3 \quad \#CC = 10$

**ORDER EQUATION:**  $185*2 = 2*25 + 4*50 + 5*24$

**NORMAL SUBGROUPS:**

H	1	5	5 <sup>2</sup>	50.4	G
G/H	G	M <sub>5,4</sub> <sup>(2)</sup>	4	2	1

$$Z = \mathcal{Z} = \Phi \quad \times 2 \quad G'$$

**Sylow subgroups:**  $[4] \times 25, [5^2]$

**Maximal subgroups:**  $[50.4], [M_{5,4}^{(2)}] \times 10$

$$100.15 = \langle A^5, B^5, C^2, D^2 = C, [A,C] = A^3, [A,D] = A, [B,D] = B^3 \rangle$$

**CLASS EQUATION:**  $100 = 1 + 2*2 + 4*5 + 5 + 10*2 + 25*2 \quad \#CC = 13$

**ORDER EQUATION:**  $265*2 = 2*5 + 4*50 + 5*24 + 10*20$

**NORMAL SUBGROUPS:**

H	1	5	5	D <sub>10</sub>	5 <sup>2</sup>	D <sub>10</sub> × 5	G
G/H	G	D <sub>5,4</sub>	M <sub>5,4</sub> <sup>(2)</sup>	D <sub>10</sub>	4	2	1

$$Z = \mathcal{Z} = \Phi \quad \quad \quad G'$$

**Sylow subgroups:**  $[4] \times 25, [5^2]$

**Maximal subgroups:**  $[D_{10} \times 5], [M_{5,4}^{(2)}] \times 5, [D_{5,4}] \times 5$

$$100.16 = \langle A^5, B^5 = A, C^2, D^2 = C, [A,C] = A^3, [A,D] = A, [B,C] = B^3A^4, [B,D] = BA \rangle$$

**CLASS EQUATION:**  $100 = 1 + 4*6 + 25*3 \quad \#CC = 10$

**ORDER EQUATION:**  $385*2 = 2*25 + 4*50 + 5*4 + 25*20$

**ORDER EQUATION:**  $385*2 = 2*25 + 4*50 + 5*4 + 25*20$

**NORMAL SUBGROUPS:**

H	1	5	25	D <sub>50</sub>	G
G/H	G	M <sub>5,4</sub> <sup>(2)</sup>	4	2	1

$$Z = \mathcal{Z} \quad \Phi \quad G'$$

**Sylow subgroups:**  $[4] \times 25, [25]$

**Maximal subgroups:**  $[D_{50}], [20.5] \times 5$

